

The highest obtainable mark is 17, the minimum passing mark is 8.5

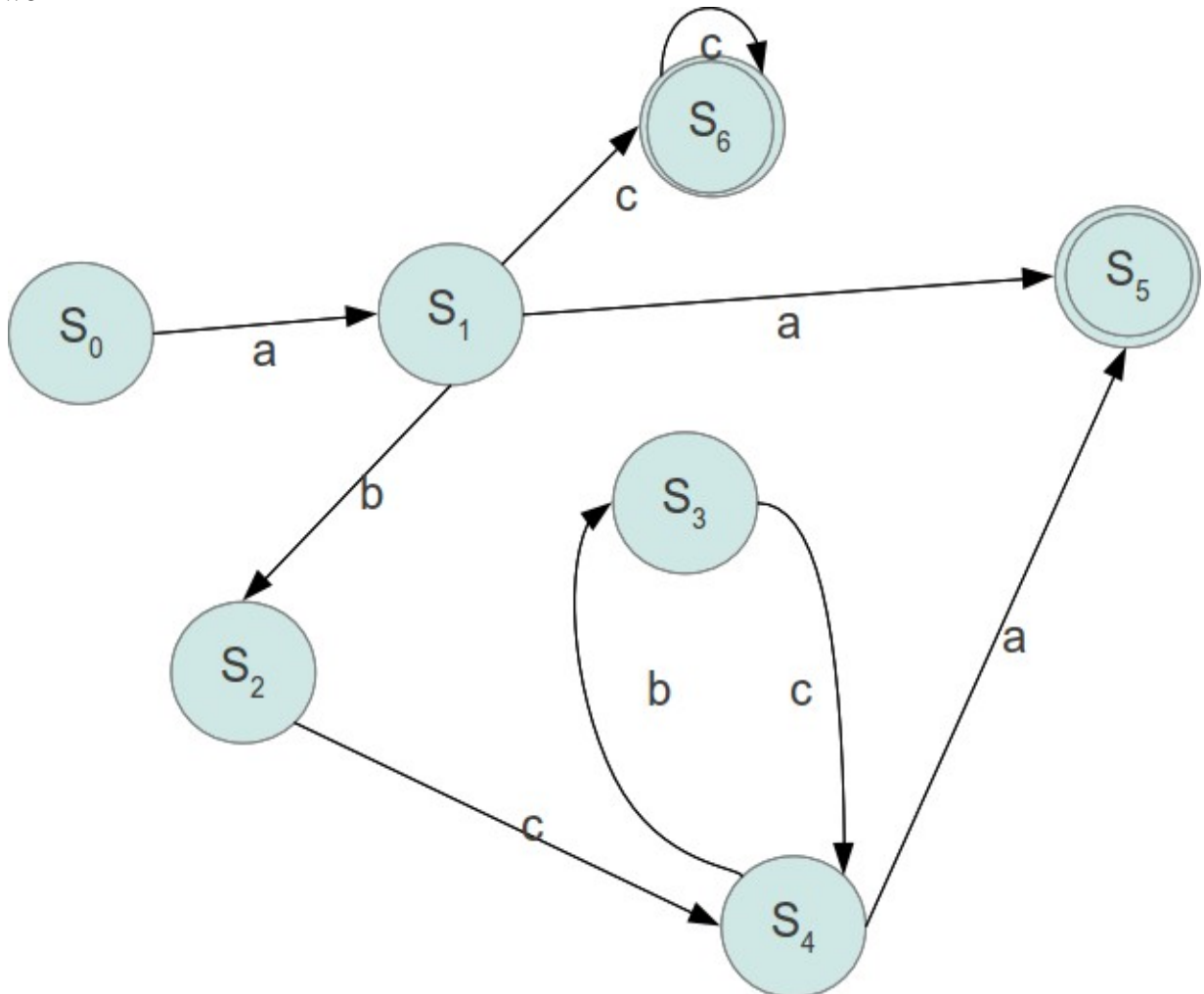
Q1: (4 points)

For the the following regular expression:

$$a(bc)^*a \mid ac(c)^*$$

1. Construct a Deterministic Finite Automaton (DFA) for the above regular expression. **(3 points)**

Answer



2. Show each step of the lexer on the string *aaaccabca*. Be sure to show the values of the important internal variables of the recognizer. There will be repeated calls to the lexer to get all tokens from the string. **(1 point)**

Answer

Input String	Start Index	Current Index	Accepting Index	Token
<u>a</u> aaccabca	0	0		
aa <u>a</u> ccabca	0	1	1	aa
aa <u>a</u> ccabca	2	2		
aa <u>a</u> ccabca	2	3	3	
aa <u>acc</u> abca	2	4	4	acc
aaacc <u>a</u> bca	5	5		
aaacc <u>a</u> bca	5	6		
aaacc <u>ab</u> ca	5	7		
aaacc <u>abca</u>	5	8	8	abca

* * *

Q2: (4 points)

Consider the following context-free grammar G_0 :

$$\begin{aligned}
 E &\rightarrow E, E \\
 E &\rightarrow E = E \\
 E &\rightarrow E[E] \\
 E &\rightarrow (E) \\
 E &\rightarrow x
 \end{aligned}$$

1. The grammar G_0 is ambiguous. Explain what this concept means, and give an example which shows that G_0 is ambiguous. **(2 points)**

Answer

Ambiguous grammars are the kind of grammars which can generate two different parse trees for the same input string.

An example to show that the above grammar is ambiguous:

$$x = x, x$$

Which can be generated in two different ways:

$$a- E \rightarrow E, E \rightarrow E = E, E \rightarrow x = x, E \rightarrow x = x, x$$

$$b- E \rightarrow E = E \rightarrow x = E \rightarrow x = E, E \rightarrow x = x, E \rightarrow x = x, x$$

2. Assume that $(E[E])$ has the highest priority, $(=)$ has the second-highest priority, and $(,)$ has the lowest priority. Rewrite G_0 to an equivalent G_1 which expresses these properties. **(1 point)**

Answer

$$\begin{aligned} E &\rightarrow E, E \mid T \\ T &\rightarrow T = T \mid F \\ F &\rightarrow F[F] \mid K \\ K &\rightarrow (E) \mid x \end{aligned}$$

3. Assume that $(=)$ is right-associative and $(,)$ is left-associative. Rewrite G_1 to an equivalent grammar G_2 which expresses these properties. **(1 point)**

Answer

$$\begin{aligned} E &\rightarrow E, T \mid T \\ T &\rightarrow F = T \mid F \\ F &\rightarrow F[F] \mid K \\ K &\rightarrow (E) \mid x \end{aligned}$$

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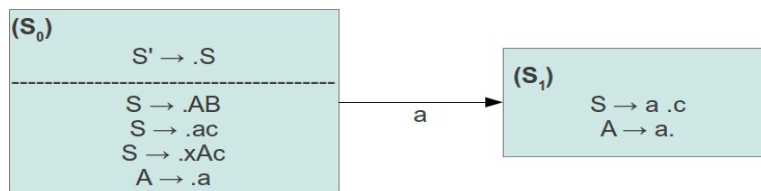
Q3: (6 points)

Consider the following augmented grammar, where S' is the start symbol and $\$$ is the special end-of-input symbol.

$$\begin{aligned} P_0 & \quad S' \rightarrow SS\$ \\ P_1 & \quad S \rightarrow AB \\ P_2 & \quad S \rightarrow a c \\ P_3 & \quad S \rightarrow x A c \\ P_4 & \quad A \rightarrow a \\ P_5 & \quad B \rightarrow b \\ P_6 & \quad B \rightarrow - \end{aligned}$$

1. Show that this grammar is not *SLR* (or, show that the *SLR* construction will fail). **(1 points)**

Answer



The *FOLLOW* of A is $\{b, c\}$ so the *Action/Goto* table of S_1 will be like:

States	Action						Goto		
	a	c	x	b	-	\$	S	A	B
S_1		s1, r4		r4					

In state S_1 we have both *shift* and *reduce*, which means this is not an *SLR* grammar.

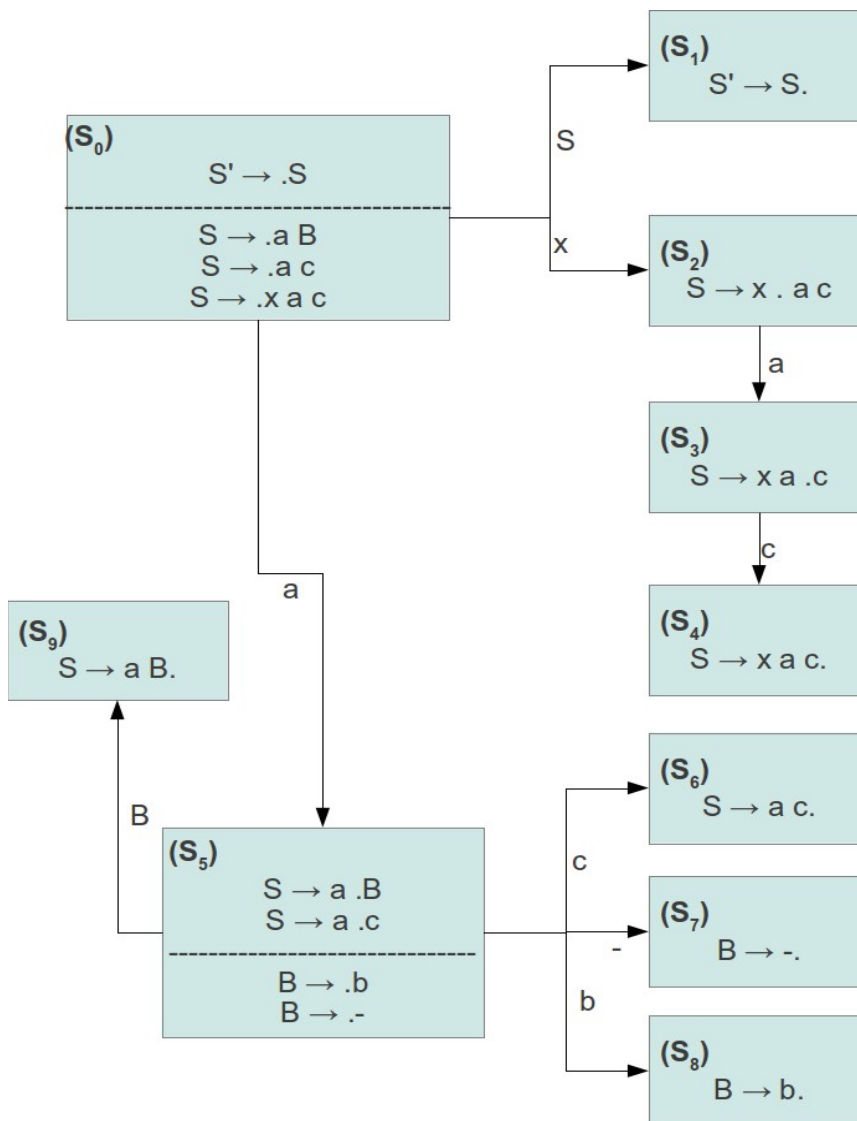
2. Rewrite the grammar to an equivalent grammar that is *SLR*. (Hint: clone or eliminate the non-terminal *A*.) Construct an *SLR* parsing table for the new grammar, including the intermediate *LR(0)* automation with states and transitions, and the *FIRST* and *FOLLOW* sets for the non-terminals. (4 points)

Answer

By eliminating the terminal *A* we will get the following grammar:

- $P_0 \quad S' \rightarrow SS$
- $P_1 \quad S \rightarrow aB$
- $P_2 \quad S \rightarrow ac$
- $P_3 \quad S \rightarrow xac$
- $P_4 \quad B \rightarrow b$
- $P_5 \quad B \rightarrow -$

The *LR(0)* DFA will look like:



The SLR table:

States	Action						Goto	
	a	c	x	b	-	\$	S	B
S ₀	s5		s2				g1	
S ₁						A		
S ₂	s3							
S ₃		s4						
S ₄						r3		
S ₅		s6		s8	s7		g9	
S ₆						r2		
S ₇						r5		
S ₈						r4		
S ₉						r1		

$$FIRST(S) = \{a, x\}, FIRST(B) = \{b, -\} \quad FOLLOW(S) = \{\$, \}, FOLLOW(B) = \{\$, \}$$

3. Show how an LR parser step by step (including changes in the stack and remaining tokens) parses the string *xac* using your SLR table. (1 point)

Answer

Stack	Input	Action
\$0	xac\$	s2: Shift on x
\$0x2	ac\$	s3: Shift on a
\$0x2a3	c\$	s4: Shift on c
\$0x2a3c4	\$	Reduce S → xac Pop xac *2, exposing 0, push S Goto(0, S)=1
\$0S1	\$	Accept

* * *

Q 4: (3 points)

Knowing that C-like languages use static scoping:

1. You are writing a C-compiler for a device that has a 2.4 GHz i7 CPU and only 256 MB of RAM. Describe an *efficient* way of processing nested scopes for your compiler. Motivate your answer. (2 points)

This is a device with a high speed and a low memory, so an efficient way for handling the nested scopes is:

- *First traverse the scope's declarations (the syntax tree) and enter them in the hash table.*
- *Type-check the statements/expressions inside the scope.*
- *Before leaving the scope, traverse the scope's declarations again and remove them from the hash table.*

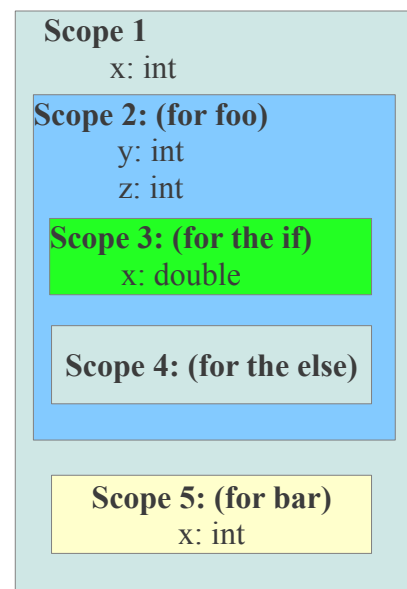
since this alternative does not use an extra memory, although it is a bit slow.

2. Identify the *scopes* and the *variable* declarations for each scope of the following C program. (1 point)

```
int x;
int foo(int y)
{
    int z;
    if (y != 0) {
        double x = 3.14;
        z = bar(x);
    } else
        z = x;
    return z;
}

int bar(void)
{
    int x = 2;
    return x;
}
```

Answer



Good Luck